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FIG. 4. Experimental hyperfine fields vs  $T/T_C$  for Pd<sub>1-x</sub>Co<sub>x</sub> alloys at 297 °K, with pressure the implicit variable.  $H_i(p)$  data are the smoothed experimental curves of Fig. 3 and  $T_C(p)$  data are taken from Table I. The right-hand ordinate is normalized to  $|H_0(p=0)| = 308$  kOe as described in the text. The dashed curve is the molecular-field spontaneous-magnetization function of spin- $\frac{1}{2}$ . The arrows indicate the direction of increasing pressure.

relation is easily calculated in the molecular-field approximation and works well if conduction-electron contributions to the impurity moment are small. For a strong response (Fe<sup>57</sup> in Ni) g lies above f, saturating more quickly as T drops below  $T_c$ , while for a weak response (Mn<sup>55</sup> in Fe) g lies below f and may be sigmoid shaped.<sup>63,60</sup> Under pressure, then, one must now consider  $\xi(p)$ , the pressure dependence of the relative host-impurity magnetic coupling. As before, the hyperfine field follows the magnetization associated with the parent atom as a function of temperature, although the latter quantity is no longer tracking the magnetization of the host. Thus

$$H_i(T) = H_0 g(T/T_C) , (4)$$

whence, using Eq. (3), the hyperfine coupling constant is  $A = H_i(T)/\mu(T) = H_0/\mu_0$ . In this picture, then, the host magnetization  $\sigma(T)$  is coupled to the local impurity magnetization  $\mu(T)$  via  $\zeta$ , and  $\mu(T)$ is in turn coupled to the impurity hyperfine field  $H_i(T)$  via A.

There are thus five phenomenological parameters whose pressure dependence is expected to be of primary importance in interpreting pressure effects on the hyperfine fields associated with welldefined localized-moment impurities in ferromagnetic hosts:  $T_C$ ,  $\sigma_0$ ,  $\mu_0$ ,  $\zeta$ , A. The pressuredependent quantities most directly related to the observed hyperfine fields are:  $T_C$ ,  $H_0 = A\mu_0$ , and  $\zeta$ . On the other hand, in homogeneous cases the relevant quantities are:  $T_C$  and  $H_0 = A\sigma_0$ , and the parameter  $\zeta$  does not appear. Information on interactions within the host are given by the pressure (or volume) dependences of  $T_C$  and  $\sigma_0$ ; the pressure dependence of  $\mu_0$ , A, and  $\zeta$  are properties of the impurity atom itself and of its interaction with the host.

## C. Results

We now show, with reference to the parameters outlined above, that it is possible to explain the essential features of the data of Fig. 4 by use of a simple molecular-field picture. Semiguantitative estimates of the pressure dependences of the relevant parameters are obtained. Quantitative determinations, however, will be seen to require further temperature-dependent data which are not currently available. In Fig. 5 we plot a family of impurity response functions  $g(T/T_c)$  for impurity spin- $\frac{1}{2}$ , parametrized by the relative host-impurity coupling constant  $\zeta$ , referenced to the host spontaneous-magnetization function  $f(T/T_c)$  of spin- $\frac{1}{2}$ , all within the molecular-field approximation.  $g(T/T_c)$ coincides with  $f(T/T_c)$  here when  $\zeta = 1.0$ . The function  $g(T/T_c)$  is related to  $f(T/T_c)$  in the molecular-field approximation according to

$$g(T/T_{c}) = B_{S'} \left( \zeta \, \frac{f(T/T_{c})}{T/T_{c}} \right) \quad , \tag{5}$$

where S' is the impurity spin and  $B_S$  is a Brillouin function.<sup>60,63</sup> The host spontaneous-magnetization function  $f(T/T_C)$  need not be expressed within the molecular-field approximation here, but can be the exact experimental function  $\sigma(T)/\sigma_0$ . Callen *et al.*<sup>61</sup> note that the molecular-field theory is much more accurate for the impurity than for the host,<sup>65</sup> so Eq. (5) should work well for  $g(T/T_C)$  even when the molecular-field theory does not give a good representation of  $f(T/T_C)$ . [Equation (5) is *exact*, however, only in the weak coupling limit.<sup>62</sup>] For simple illustrative purposes in Fig. 5 we use the molecular-field theory for f as well as for g (see Appen<u>7</u> dix).

By considering the functions  $g(T/T_c)$  of Fig. 5 to represent possible values of  $H_i(T)/H_0$  according to Eqs. (4) and (5), a series of hypothetical pressure-dependent curves can be generated by use of (i) the values  $T/T_c(p)$  for each alloy from the data of Table I with  $T = \text{const} = 297 \,^{\circ}\text{K}$  (as was done in Fig. 4) and (ii) an assumed  $\zeta(p)$ . For example,  $\xi(p) = \text{constant implies that all curves } H_i(T, p)/$  $H_0(p)$  coincide with the same function  $g(T/T_c)$  as  $T/T_{c}(p)$  decreases with pressure for each alloy. The dashed segments in Fig. 5 illustrate the effect of a linear decrease of  $\zeta$  with pressure, from  $\zeta = 1.0$  at 0 kbar to  $\zeta = 0.6$  at 180 kbar. For purposes of comparison with the data of Fig. 4, however, it is necessary to convert the dashed curves of Fig. 5 to the form  $H_i(T, p)$  vs  $T/T_c(p)$ , i.e., to multiply each dashed segment by  $H_0(p)$ . The pressure dependence of  $H_0$ is most readily determined for the alloy with lowest  $T/T_c$ , since  $H_i(T)$  there has greatest sensitivity to changes of  $H_0$ .  $H_0(p)$  has thus been "fitted" for Pd<sub>0.85</sub>Co<sub>0.15</sub> by requiring that the model curve reproduce the experimental ratio  $[H_i(p=180)/$  $H_i(p=0)$ ] = 1.08 for this alloy (pressure units in kbar), with a linear pressure dependence. The solid segments in Fig. 5 show the effect of applying this same  $H_0(p)$  to all four alloys. The righthand ordinate of Fig. 5 should be compared to the right-hand ordinate of Fig. 4. The similarities to the experimental curves of Fig. 4 are apparent: The x = 0.09 alloy shows a very dramatic pressure effect; the various  $H_i(T, p)$  segments are not continuous, with the x=0.08 curve lying below the x = 0.09 curve and the high-pressure region of the x = 0.12 curve falling below the low-pressure overlapping  $T/T_c$  region of the x=0.15 curve; the

over-all increase of  $|H_i|$  is greater for the x=0.12alloy than for x = 0.15 and greater for x = 0.09 than for x = 0.08; all curves have qualitatively the correct shapes, increasing most rapidly at the lower pressures and tending to level off at the higher pressures. The values of the two pressure-dependent parameters employed in Fig. 5 are  $d \ln \zeta/dp$  $= -2.8 \times 10^{-3}$ /kbar and  $d \ln H_0/dp = +1.1 \times 10^{-3}$ /kbar, the same for all alloys. The most glaring fault of the model curves of Fig. 5 is the insufficient depression of the x = 0.08 curve below the x = 0.09curve. This difficulty can be rectified somewhat by assuming a larger negative pressure dependence to  $\zeta$ , and the effect of doing so is shown in Fig. 6, where  $\zeta = 0.5$  at 180 kbar and  $H_0(p)$  is determined by the same criterion as above. The situation is indeed improved for x = 0.08 and x = 0.09 but is worsened for x=0.12 and x=0.15, because the experimental curves do not show a decrease of  $|H_i|$ at the highest pressures. In Fig. 6,  $d \ln \zeta/dp$  $= -3.7 \times 10^{-3}$ /kbar and  $d \ln H_0 / dp = +1.7 \times 10^{-3}$ /kbar. The model curves of Figs. 5 and 6 are not de-

tailed quantitative reproductions of the experimental data for several reasons, although in view of the simplicity of the molecular-field model used and the paucity of pressure-dependent parameters employed the qualitative picture is indeed satisfactory. For example, we have included no variation of the parameters  $\zeta(p)$  and  $H_0(p)$  with composition, and have moreover assumed linear pressure dependences for these quantities. The major obstacle to a more quantitative analysis of the present pressure-dependent data, however, lies in the lack of a satisfactory p = 0 "baseline" for each alloy from which a realistic set of the  $\zeta$ -dependent functions  $g(T/T_C)$  can be obtained from Eq. (5) or from



FIG. 5. Model curves of normalized hyperfine fields vs  $T/T_C$ . Light lines: molecular-field impurity response functions, parametrized by  $\xi$  as described in the text. Dashed lines: hypothetical pressure-dependent impurity response curves using  $T_C(\phi)$  from Table I and  $\xi(\phi)$  as described in the text. Heavy lines: dashed lines modified by pressure-dependent  $H_0(\phi)$  as described in the text, representing normalized hyperfine field curves to be compared to the right-hand ordinate of Fig. 4.